



ИСОИ ИПО



SAMARA UNIVERSITY

# The optical vortices structure controlling by changing the height of silicon ring gratings using high-performance computer systems

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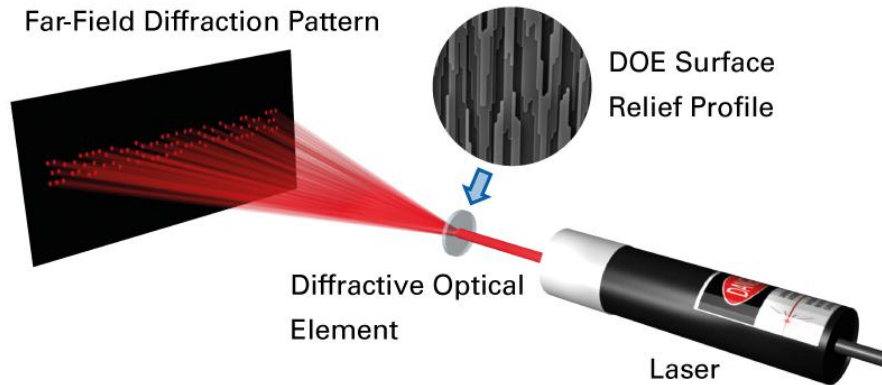
*Image Processing Systems Institute of RAS – Branch of the  
FSRC "Crystallography and Photonics" RAS*

Samara, Russia

2022



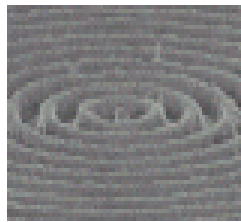
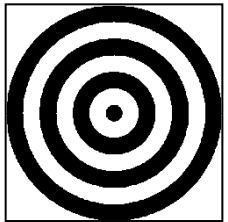
# DIFFRACTIVE OPTICAL ELEMENTS (DOE)



- **DOE is designed to form the required distribution** of the electromagnetic field.
- **The main difficulty in the synthesis** of DOEs is the **solution of the inverse diffraction problem**.
- **Examples:** Fresnel lens, diffraction gratings, interference holograms, synthesized diffraction relief, metasurfaces, depicting and non-depicting DOE.

## Diffractive axicon:

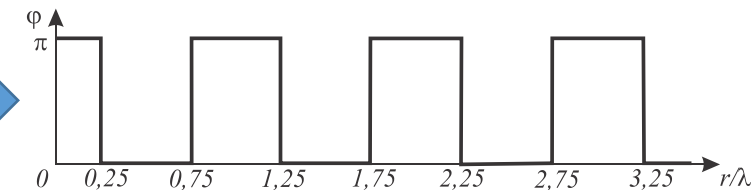
Structure of the element



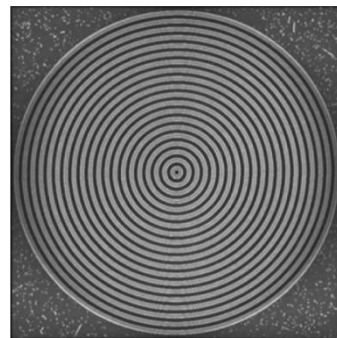
The complex transmission function

$$\tau_b(r) = \begin{cases} \exp\{i \arg[\cos(k\alpha_0 r)]\}, & r \leq R, \\ 0, & r > R. \end{cases}$$

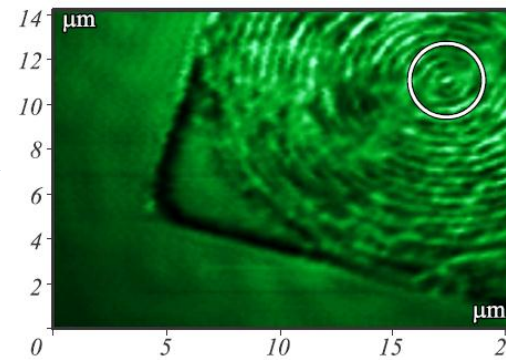
The radial cross section of the phase element



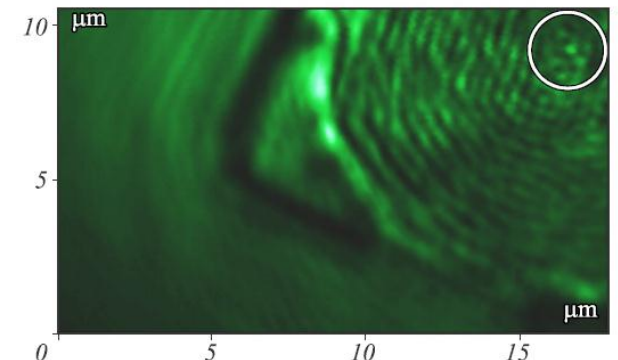
SEM image of axisymmetric binary axicon



linearly polarized beam



circularly polarized beam



**Experimental demonstration** on the optical axis with high-numerical-aperture binary axicons illuminated by linearly and circularly polarized beams:

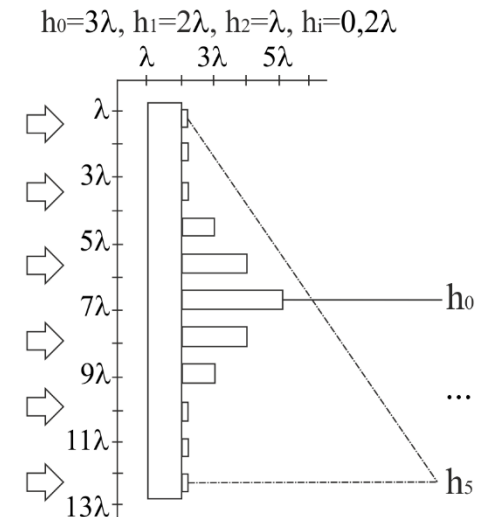
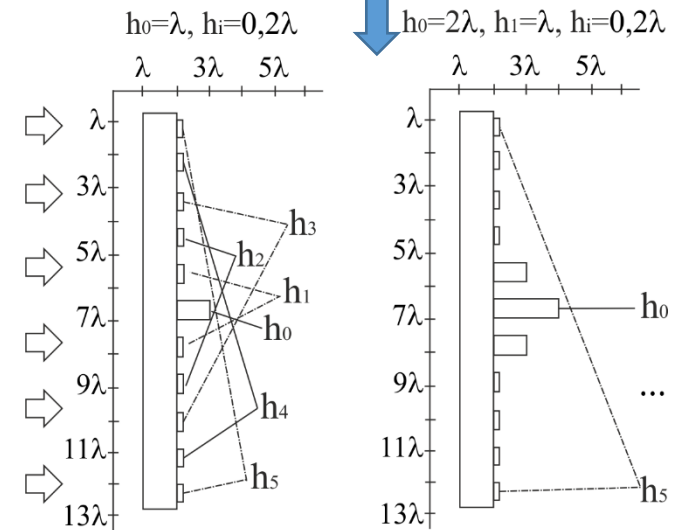
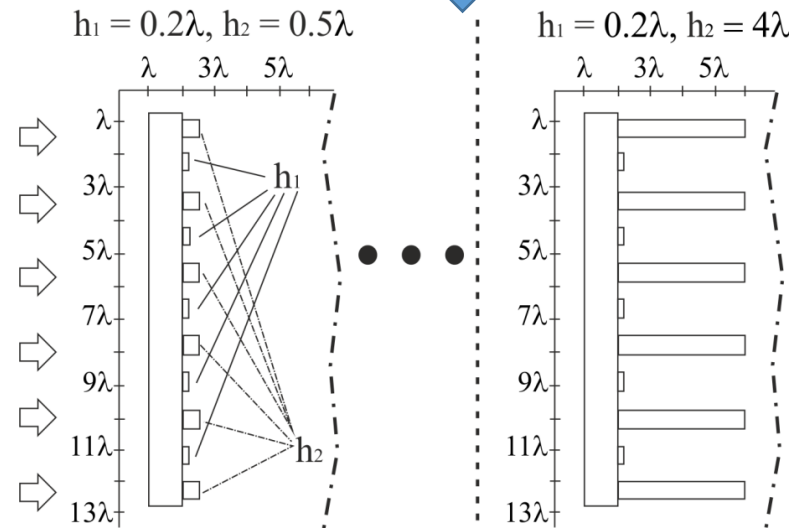
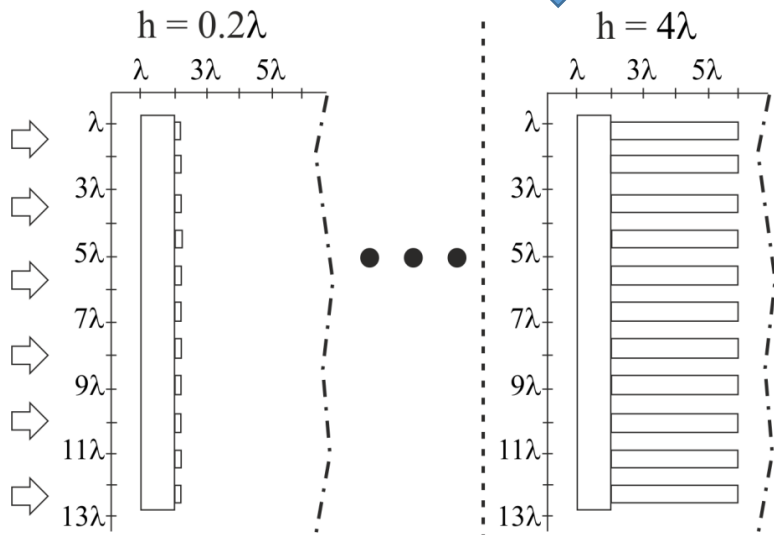
Khonina, S. N., Karpeev, S. V., Alferov, S. V., **Savelyev, D. A.**, Laukkanen, J., & Turunen, J. (2013). Experimental demonstration of the generation of the longitudinal E-field component on the optical axis with high-numerical-aperture binary axicons illuminated by linearly and circularly polarized beams. *Journal of Optics*, 15(8), 085704.





# RING GRATINGS AND INPUT BEAMS

## Ring Gratings



The examples of profiles of considered silicon ring gratings with different height  $h_i$

The examples of profiles of the considered **silicon axicons** with minimum and maximum heights (from  $0.2\lambda$  to  $4\lambda$ )

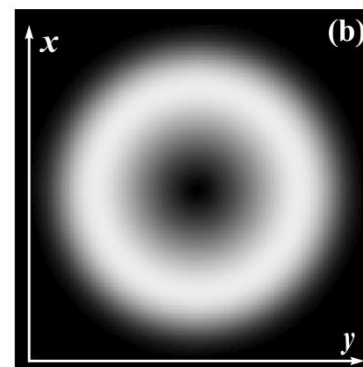
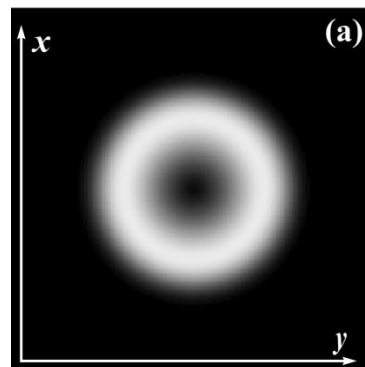
The examples of profiles of the considered **silicon ring gratings** with minimum and maximum heights  $h_2$

### The input beams:



(a)  $\sigma = 5 \mu\text{m}$  and (b)  $\sigma = 7.3 \mu\text{m}$

$$A(r, \varphi) = r \cdot \exp\left[-\frac{r^p}{2\sigma^p}\right] \cdot e^{i\varphi}, \quad p = 6.$$





## SIMULATION PARAMETERS

- **The wavelength**  $\lambda = 1.55 \mu\text{m}$ .
- **The size** of the computational domain  $x, y, z$  in  $[-5.7\lambda; 5.7\lambda]$ .
- **The thickness** of the **absorbing layer** PML  $\sim \lambda$ ,
- **The sampling step** of space –  $\lambda/30$ , the sampling step of time –  $\lambda/(60c)$ , where  $c$  is the light velocity.
- The Laguerre-Gauss mode (1,0) (**optical vortex**) with different beam width was considered as **input laser beams**.
- **Circular polarization** (the *sign* of circular polarization *is opposite* to the *sign* of the *introduced vortex phase singularity*).
- **The numerical aperture** (NA) of the focusing binary axicon was **0.95** (*grating period*  $1,05\lambda$ ).
- **The refractive index** of the optical element is  **$n = 3.47$** .
- **The height of the relief** of the annular grating **changed from  $0.2\lambda$  to  $4\lambda$** .
- **Diffraction modeling (3D)** was performed using the **finite difference time domain (FDTD)** method.
- **For calculations** used a free-software package **Meep**.
- **The calculations** were carried out on **computing cluster** with a 950 GFlop power.







## CLUSTER "SERGEY KOROLEV"



### General characteristics:

- The total number of processors / cores: 360/1992;
- Total number of graphics processors / cores: 5/4216;
- Total Memory: 6672 GB;
- System network: QLogic / Voltaire InfiniBand DDR, QDR;
- Type of control support network: Gigabit Ethernet;
- Operating system: Red Hat Enterprise Linux.



### **The computing part includes:**

- 112 BladeCenter HS22 blade server computing with 2x Intel Xeon X5560;
- 28 HS23 blade servers with 2x Intel Xeon E5-2665;
- 14 HS23 blade servers with 2x Intel Xeon E5-2680v2;
- 14 HS22 blade servers with 24 GB of memory on the server with 2x Intel Xeon X5670;
- 8 HS22 blade servers with 96 GB memory on the server with 2x Intel Xeon X5670;
- 2 HS22 blade servers with graphics cards Nvidia Tesla 2070;
- SMP server, CPU – 4x Intel Xeon E7-4860, GPGPU – Nvidia Tesla K20c.
- Etc...



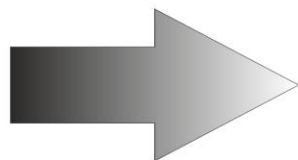
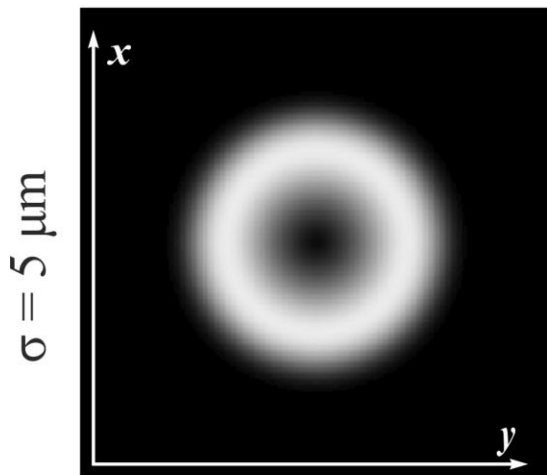
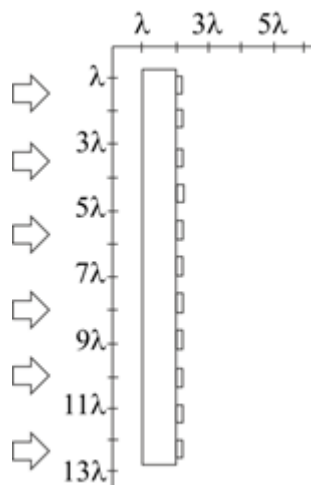


# LASER RADIATION PROPAGATION THROUGH SILICON AXICONS FROM $h = 0.2\lambda$

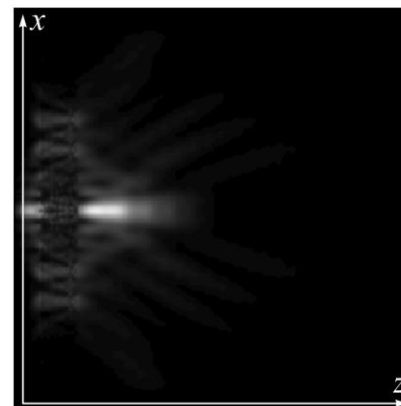
$$h = \frac{\pi}{k(n-1)} = 0.202429\lambda \approx 0.2\lambda, \text{ where } k = 2\pi/\lambda \text{ is wave number,}$$

$\lambda$  is wavelength of laser radiation, and  $n$  is refractive index.

The relief height corresponded to the phase jump  $\pi$  radians.

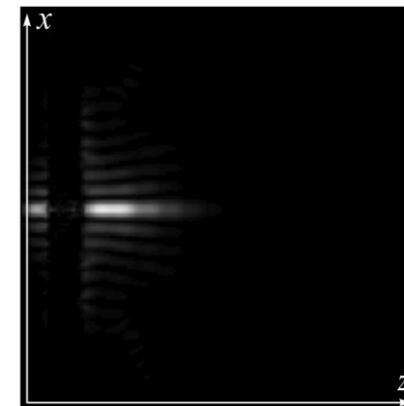


The total intensity

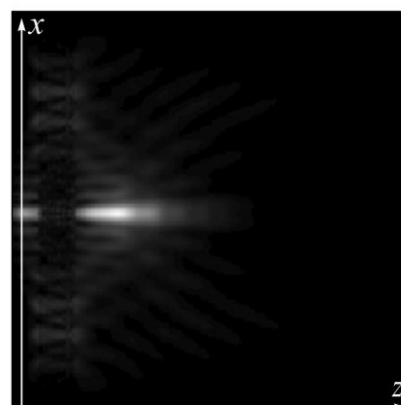
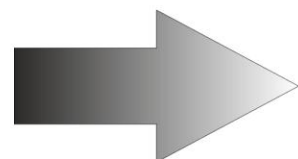
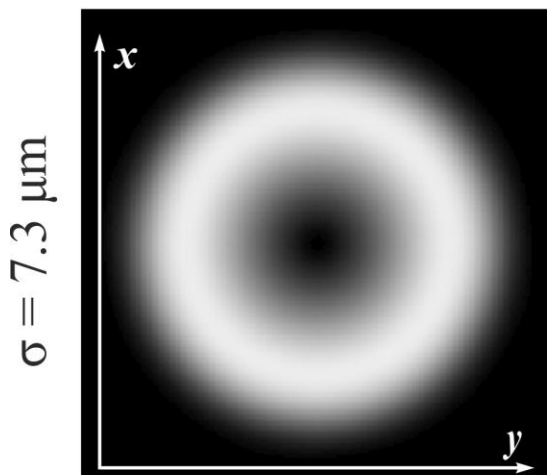


FWHM =  $0.5\lambda$ , DOF =  $1.92\lambda$

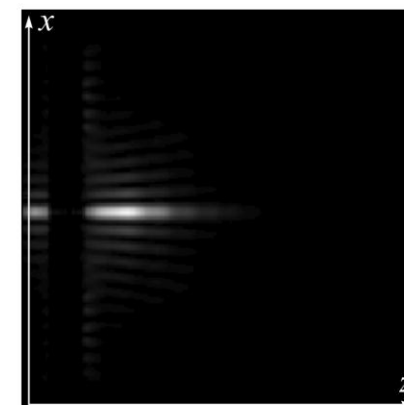
The intensity of the longitudinal component



FWHM =  $0.44\lambda$ , DOF =  $1.92\lambda$



FWHM =  $0.57\lambda$ , DOF =  $2.53\lambda$



FWHM =  $0.44\lambda$ , , DOF =  $2.53\lambda$

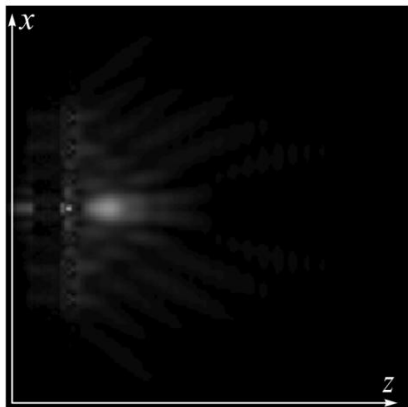




# LASER RADIATION PROPAGATION THROUGH SILICON AXICONS FROM $h = 0.5\lambda$ TO $h = 4\lambda$ , TOTAL INTENSITY

$h = 0.5\lambda$

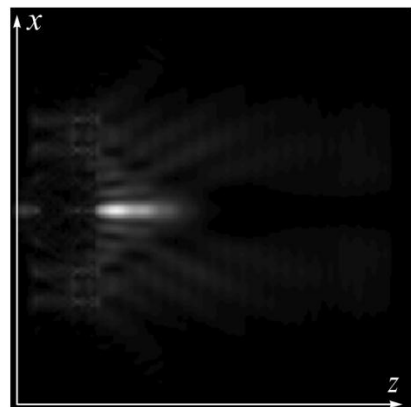
(a)



FWHM =  $0.91\lambda$ , DOF =  $1.48\lambda$

$h = \lambda$

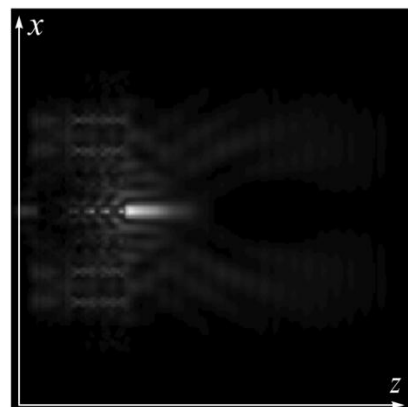
(b)



FWHM =  $0.47\lambda$ , DOF =  $1.94\lambda$

$h = 2\lambda$

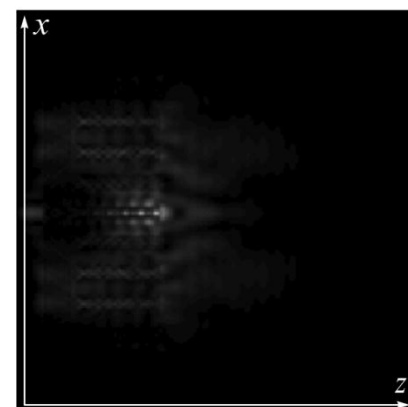
(c)



FWHM =  $0.38\lambda$ , DOF =  $1.21\lambda$

$h = 3\lambda$

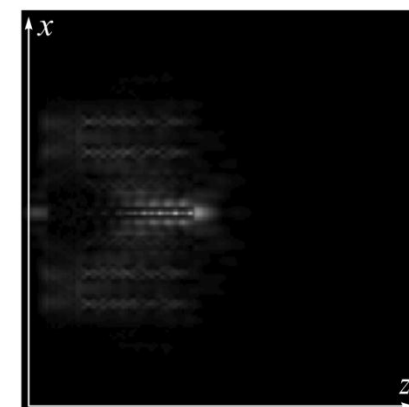
(d)



FWHM =  $0.51\lambda$ , DOF =  $0.37\lambda$

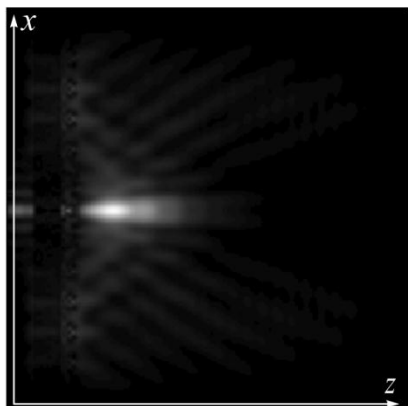
$h = 4\lambda$

(e)



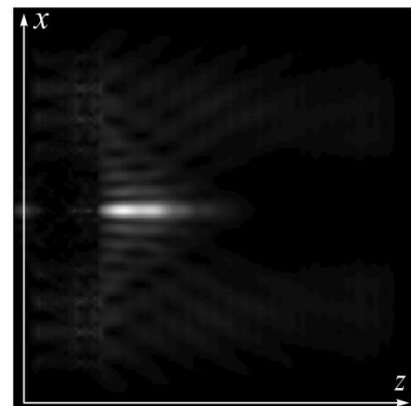
FWHM =  $0.48\lambda$ , DOF =  $0.54\lambda$

(f)



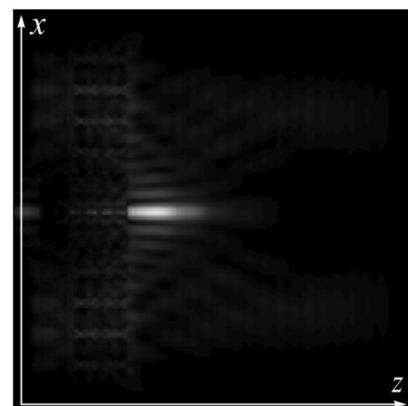
FWHM =  $0.72\lambda$ , DOF =  $2.34\lambda$

(g)



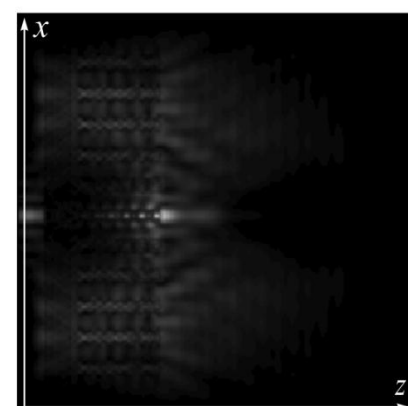
FWHM =  $0.46\lambda$ , DOF =  $2.27\lambda$

(h)



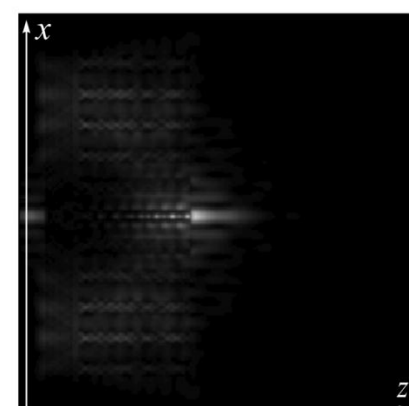
FWHM =  $0.44\lambda$ , DOF =  $1.94\lambda$

(i)



FWHM =  $0.45\lambda$ , DOF =  $0.75\lambda$

(j)



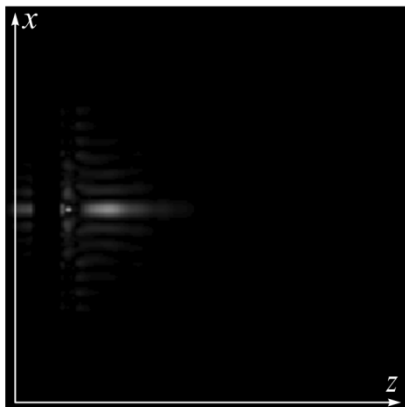
FWHM =  $0.44\lambda$ , DOF =  $1.07\lambda$



# LASER RADIATION PROPAGATION THROUGH SILICON AXICONS FROM $h = 0,5\lambda$ TO $h = 4\lambda$ , INTENSITY OF THE LONGITUDINAL COMPONENT

$h = 0.5\lambda$

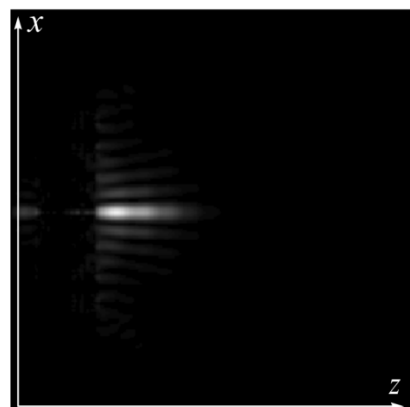
(a)



FWHM<sub>z</sub> = 0.45λ, DOF<sub>z</sub> = 1.48λ

$h = \lambda$

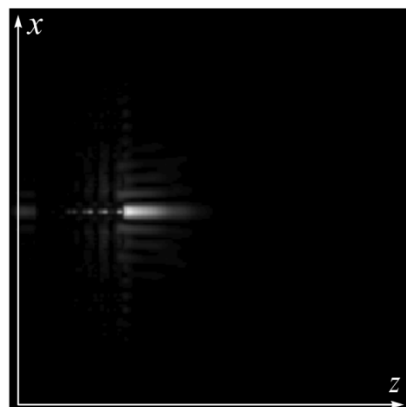
(b)



FWHM<sub>z</sub> = 0.44λ, DOF<sub>z</sub> = 1.94λ

$h = 2\lambda$

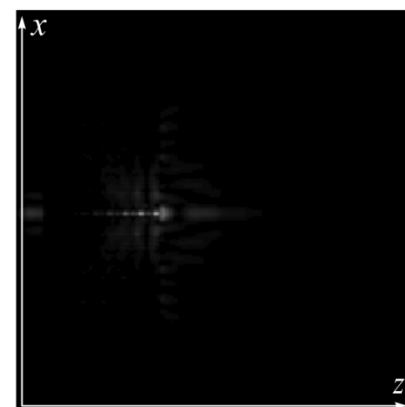
(c)



FWHM<sub>z</sub> = 0.37λ, DOF<sub>z</sub> = 1.2λ

$h = 3\lambda$

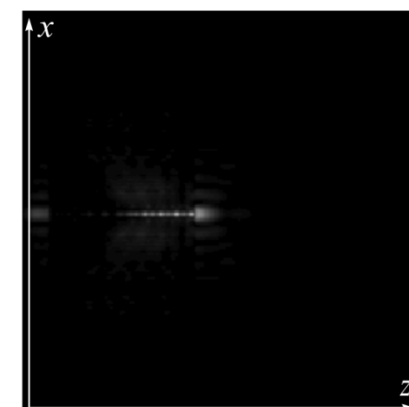
(d)



FWHM<sub>z</sub> = 0.46λ, DOF<sub>z</sub> = 0.36λ

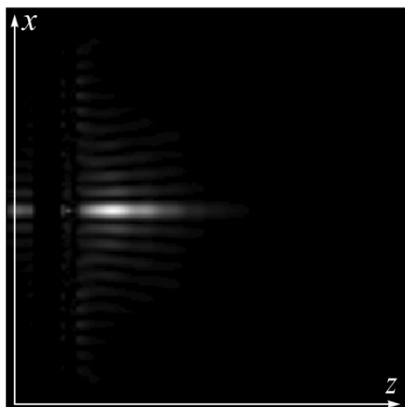
$h = 4\lambda$

(e)



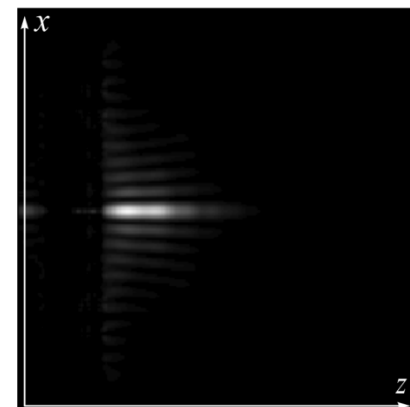
FWHM<sub>z</sub> = 0.44λ, DOF<sub>z</sub> = 0.53λ

(f)



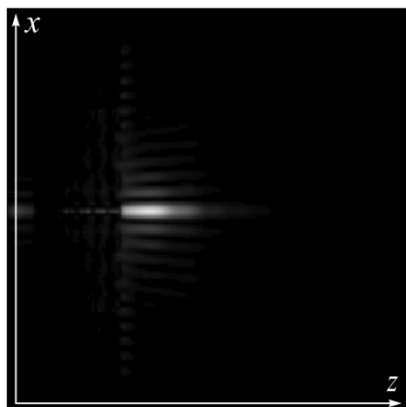
FWHM<sub>z</sub> = 0.43λ, DOF<sub>z</sub> = 2.33λ

(g)



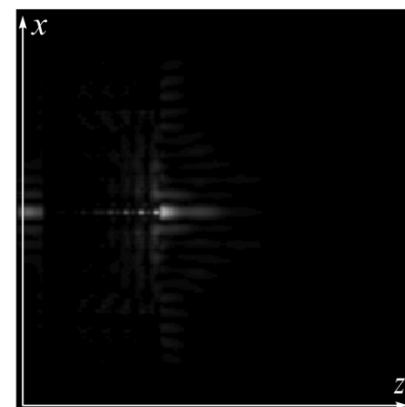
FWHM<sub>z</sub> = 0.42λ, DOF<sub>z</sub> = 2.27λ

(h)



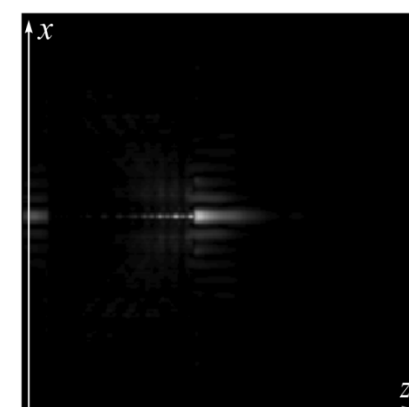
FWHM<sub>z</sub> = 0.4λ, DOF<sub>z</sub> = 1.94λ

(i)



FWHM<sub>z</sub> = 0.44λ, DOF<sub>z</sub> = 0.74λ

(j)



FWHM<sub>z</sub> = 0.4λ, DOF<sub>z</sub> = 1.06λ



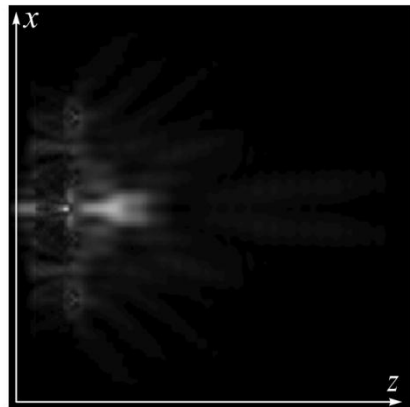




# LASER RADIATION PROPAGATION THROUGH SILICON RING GRATINGS FROM $h = 0,5\lambda$ TO $h = 4\lambda$ , TOTAL INTENSITY

$h = 0.5\lambda$

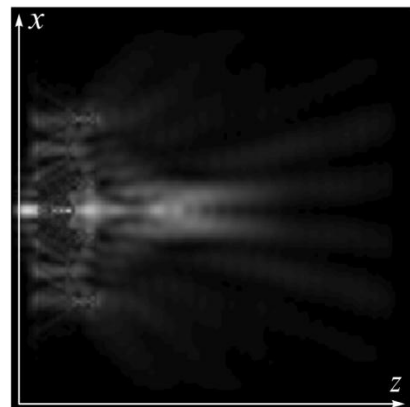
(a)



FWHM =  $0.84\lambda$ , DOF =  $1.88\lambda$

$h = \lambda$

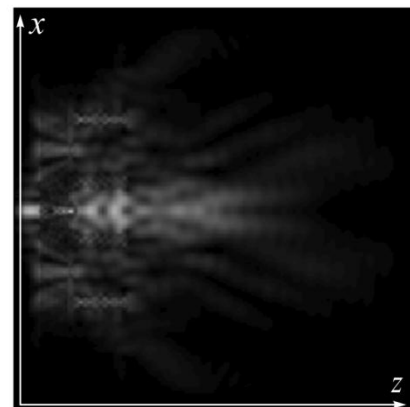
(b)



FWHM =  $1.49\lambda$ , DOF =  $1.93\lambda$

$h = 2\lambda$

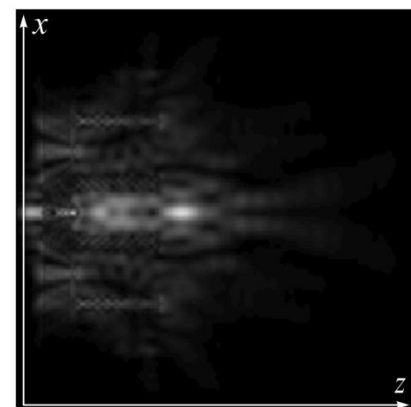
(c)



FWHM =  $0.73\lambda$ , DOF =  $0.75\lambda$

$h = 3\lambda$

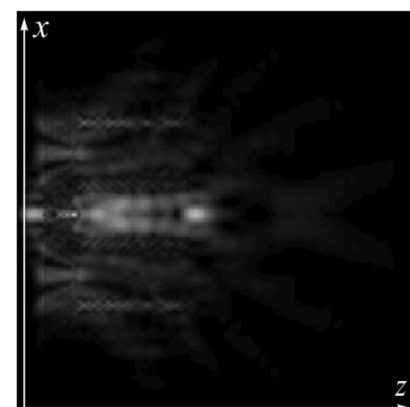
(d)



FWHM =  $0.6\lambda$ , DOF =  $1.32\lambda$

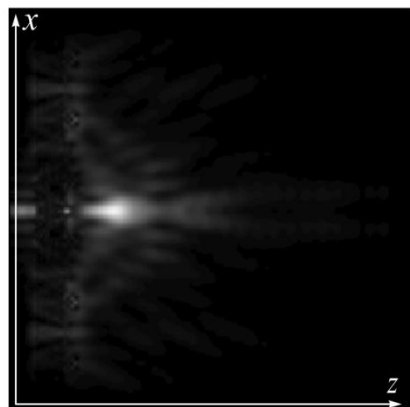
$h = 4\lambda$

(e)



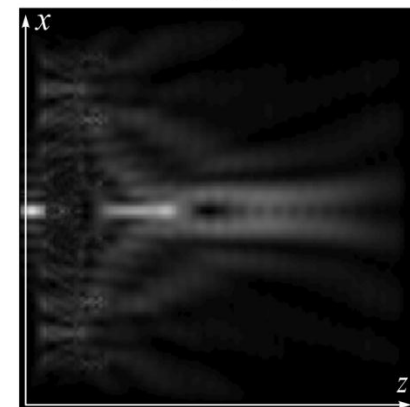
FWHM =  $0.56\lambda$ , DOF =  $0.86\lambda$

(f)



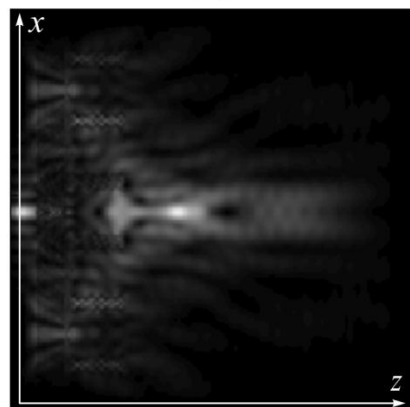
FWHM =  $0.86\lambda$ , DOF =  $1.73\lambda$

(g)



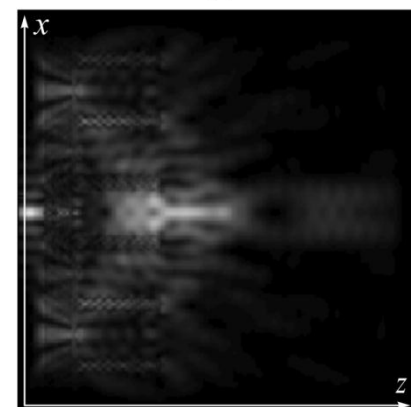
FWHM =  $0.72\lambda$ , DOF =  $2.97\lambda$

(h)



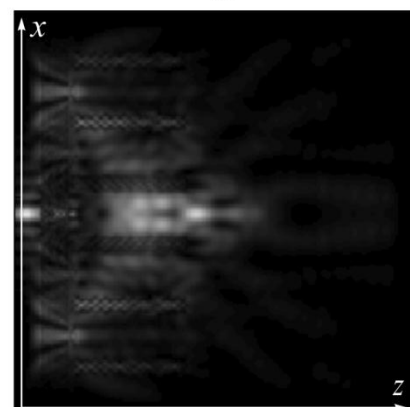
FWHM =  $0.59\lambda$ , DOF =  $1.83\lambda$

(i)



FWHM =  $0.65\lambda$ , DOF =  $4.65\lambda$

(j)



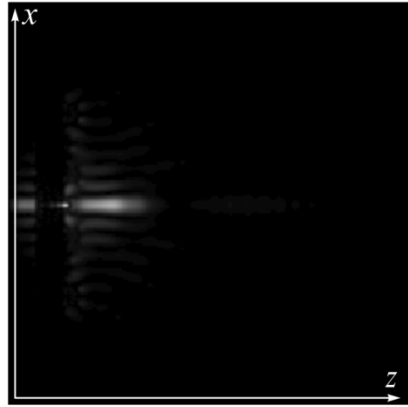
FWHM =  $0.6\lambda$ , DOF =  $1.08\lambda$



# LASER RADIATION PROPAGATION THROUGH SILICON RING GRATINGS FROM $h = 0,5\lambda$ TO $h = 4\lambda$ , INTENSITY OF THE LONGITUDINAL COMPONENT

$h = 0.5\lambda$

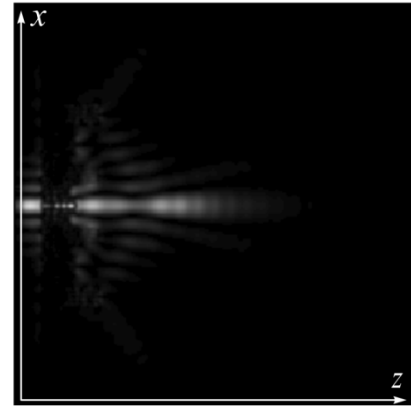
(a)



$\text{FWHM}_z = 0.45\lambda$ ,  $\text{DOF}_z = 1.86\lambda$

$h = \lambda$

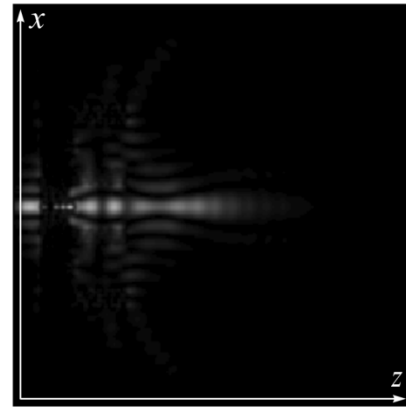
(b)



$\text{FWHM}_z = 0.44\lambda$ ,  $\text{DOF}_z = 1.92\lambda$

$h = 2\lambda$

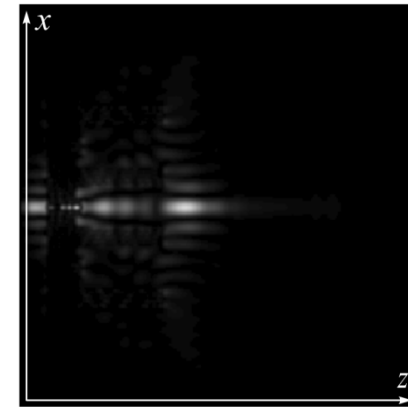
(c)



$\text{FWHM}_z = 0.47\lambda$ ,  $\text{DOF}_z = 0.75\lambda$

$h = 3\lambda$

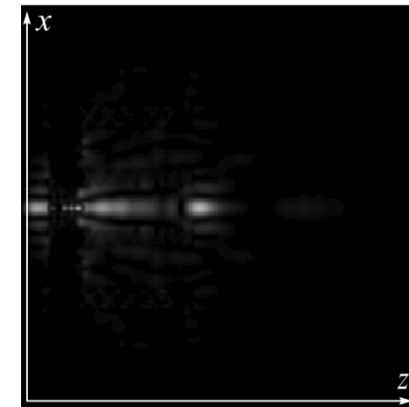
(d)



$\text{FWHM}_z = 0.45\lambda$ ,  $\text{DOF}_z = 1.31\lambda$

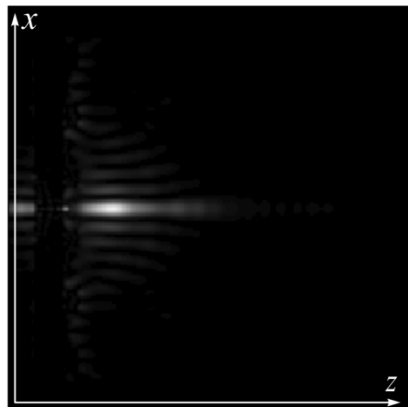
$h = 4\lambda$

(e)



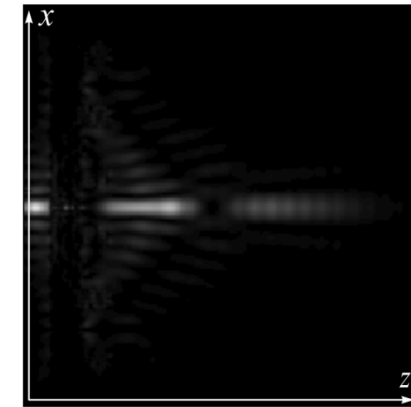
$\text{FWHM}_z = 0.46\lambda$ ,  $\text{DOF}_z = 0.86\lambda$

(f)



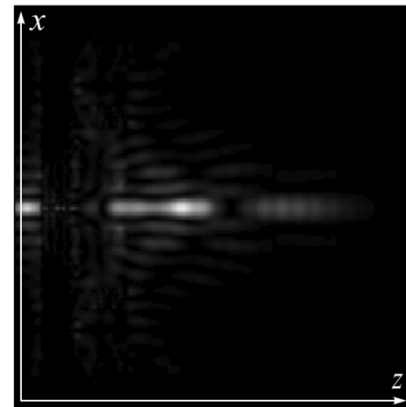
$\text{FWHM}_z = 0.44\lambda$ ,  $\text{DOF}_z = 1.73\lambda$

(g)



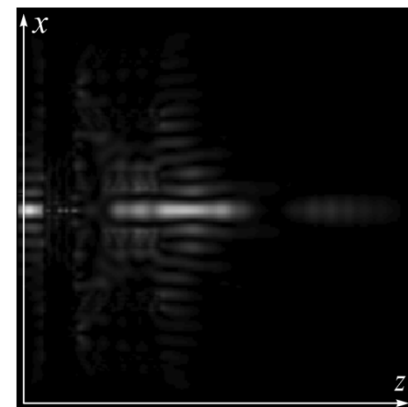
$\text{FWHM}_z = 0.49\lambda$ ,  $\text{DOF}_z = 2.95\lambda$

(h)



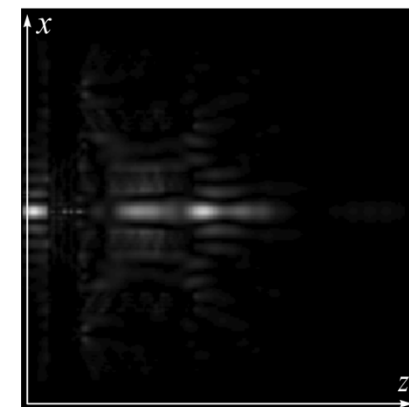
$\text{FWHM}_z = 0.48\lambda$ ,  $\text{DOF}_z = 3.3\lambda$

(i)



$\text{FWHM}_z = 0.44\lambda$ ,  $\text{DOF}_z = 4.64\lambda$

(j)

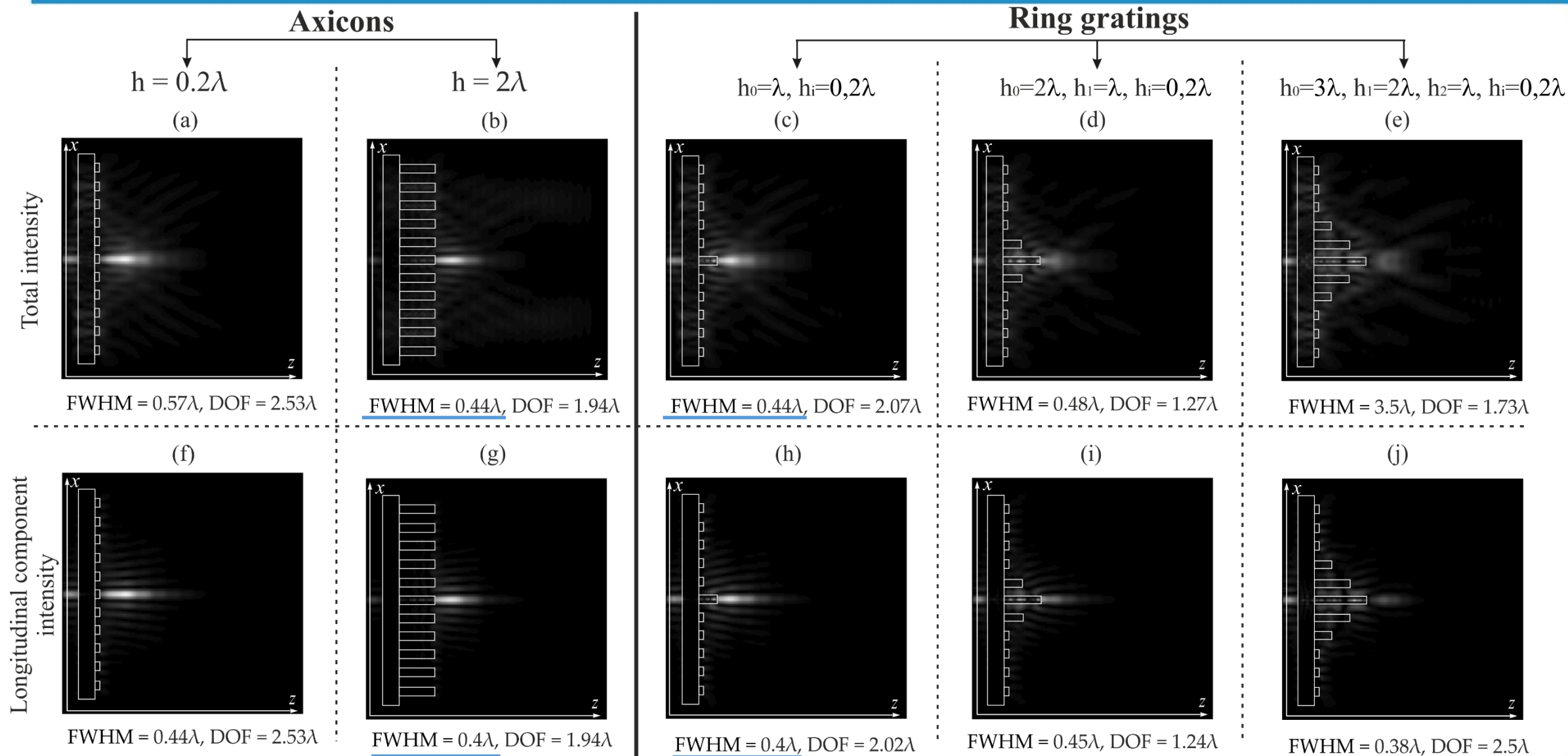


$\text{FWHM}_z = 0.46\lambda$ ,  $\text{DOF}_z = 1.07\lambda$





# LASER RADIATION PROPAGATION ON RING GRATINGS WITH VARIABLE RELIEF HEIGHT, $\sigma = 7.3 \mu\text{m}$





### Conclusions:

- The diffraction of **optical vortices with circular polarization** with different widths on **silicon ring gratings and diffractive axicons** by the finite difference time domain method were simulated.
- **The heights** of individual grating rings **were varied**.
- **The smallest focal spot size was obtained for a silicon diffractive axicon at a relief height  $h = 2\lambda$  for a laser beam with  $\sigma = 5 \mu\text{m}$  ( $\text{FWHM} = 0.38\lambda$ ,  $\text{FWHM}_z = 0.37\lambda$ ), which is better than the action of a diffractive axicon with a height  $h = 0.2\lambda$  ( $\text{FWHM} = 0.5\lambda$ ,  $\text{FWHM}_z = 0.44\lambda$ ) by 24%.**
- The results of numerical simulation for ring gratings **with different heights  $h_i$**  (increase in center height from  $\lambda$  to  $3\lambda$ ) showed that, in the general case, an **increase in height leads to the formation of a maximum inside the element**.
- **The largest light needle length** was obtained for silicon ring gratings (laser beam width  $\sigma = 7.3 \mu\text{m}$ ) **at a height  $h_2 = 3\lambda$  and  $h_1 = 0.2\lambda$  ( $\text{DOF} = 4.65\lambda$ )**, which is **83.8% longer** than the light needle of a diffractive axicon with a height  $h = 0.2\lambda$ .

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**THANK YOU**

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